

Data Mining and Knowledge Discovery

Knowledge Discovery and Knowledge Management in e-Science

Petra Kralj Novak

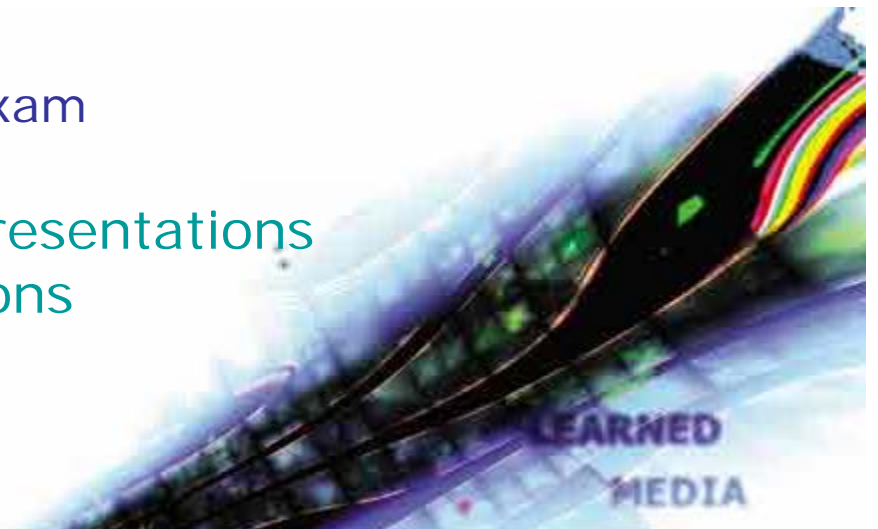
Petra.Kralj.Novak@ijs.si

Practice, 2008/11/12

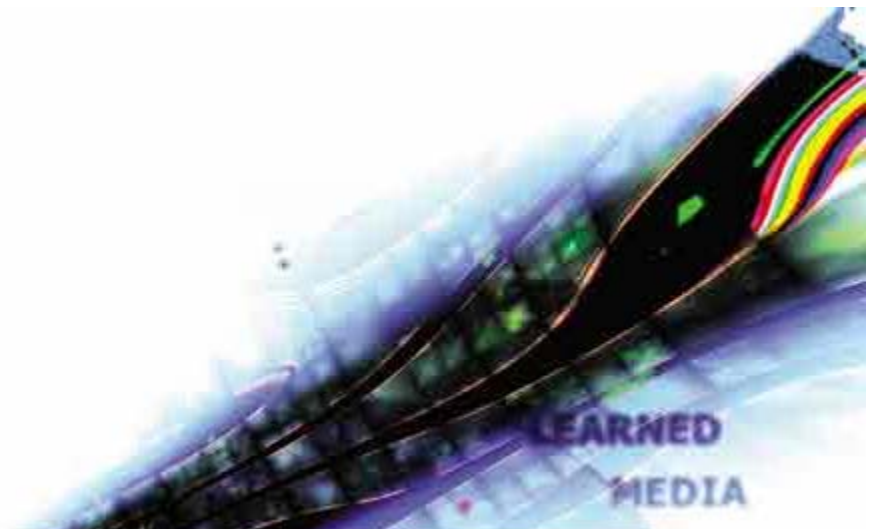


Practice plan

- 2008/10/22: Predictive data mining
 - Decision trees
 - Naïve Bayes classifier
 - Evaluating classifiers (separate test set, cross validation, confusion matrix, classification accuracy)
 - Predictive data mining in Weka
- 2008/11/11: Numeric prediction and descriptive data mining
 - Regression models
 - Regression models and evaluation in Weka
- 2008/11/12: Descriptive data mining
 - Association rules
 - Descriptive data mining in Weka
 - Discussion about seminars and exam
- 2008/12/1: Written exam
- 2008/12/8: Seminar proposals presentations
- 2009/01/14: Seminar presentations



Association Rules



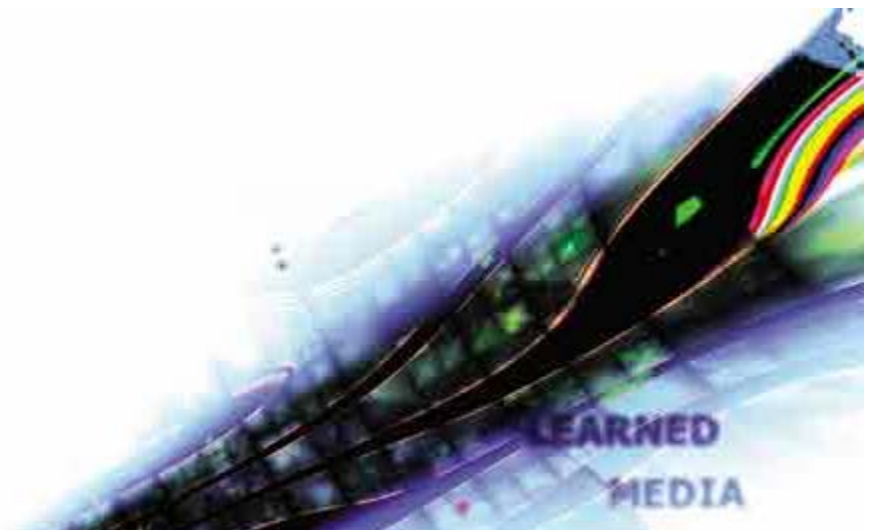
Association rules

- Rules $X \rightarrow Y$, X, Y conjunction of items
- Task: Find **all** association rules that satisfy minimum support and minimum confidence constraints
- **Support:**
$$\text{Sup}(X \rightarrow Y) = \#XY/\#D \cong p(XY)$$
- **Confidence:**
$$\text{Conf}(X \rightarrow Y) = \#XY/\#X \cong p(XY)/p(X) = p(Y|X)$$

Association rules - algorithm

1. generate frequent itemsets with a minimum support constraint
2. generate rules from frequent itemsets with a minimum confidence constraint

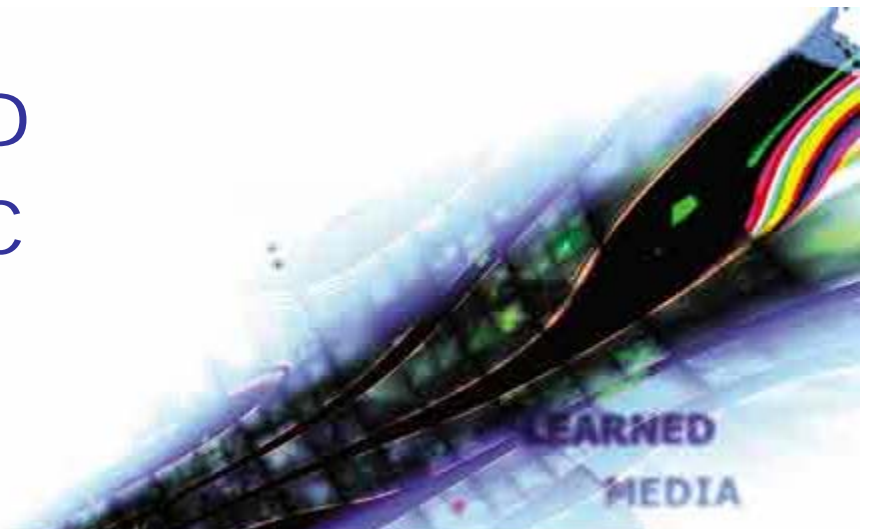
* Data are in a transaction database



Association rules – transaction database

Items: **A**=apple, **B**=banana,
C=coca-cola, **D**=doughnut

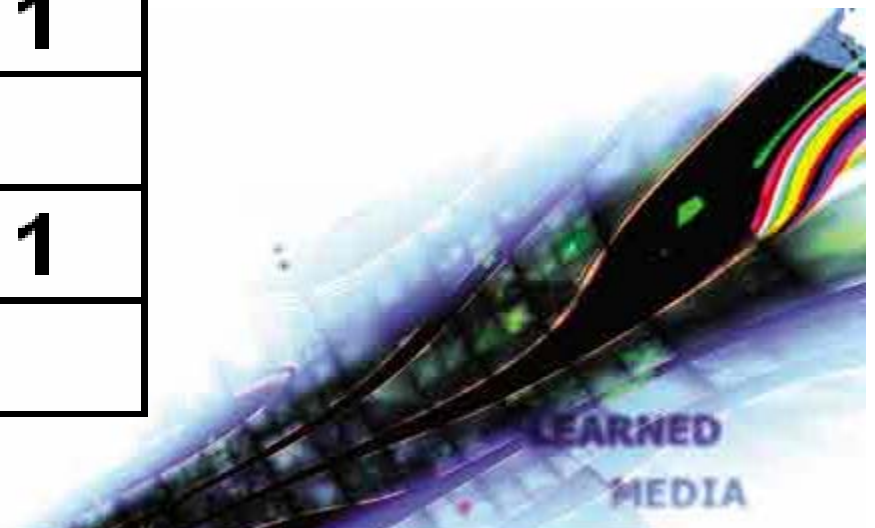
- Client 1 bought: A, B, C, D
- Client 2 bought: B, C
- Client 3 bought: B, D
- Client 4 bought: A, C
- Client 5 bought: A, B, D
- Client 6 bought: A, B, C



Frequent itemsets

- Generate frequent itemsets with support at least 2/6

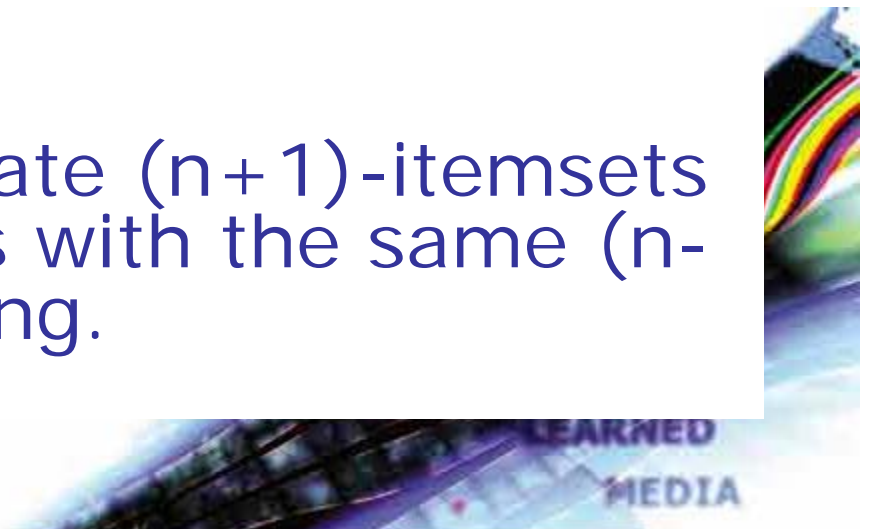
A	B	C	D
1	1	1	1
	1	1	
	1		1
1		1	
1	1		1
1	1	1	



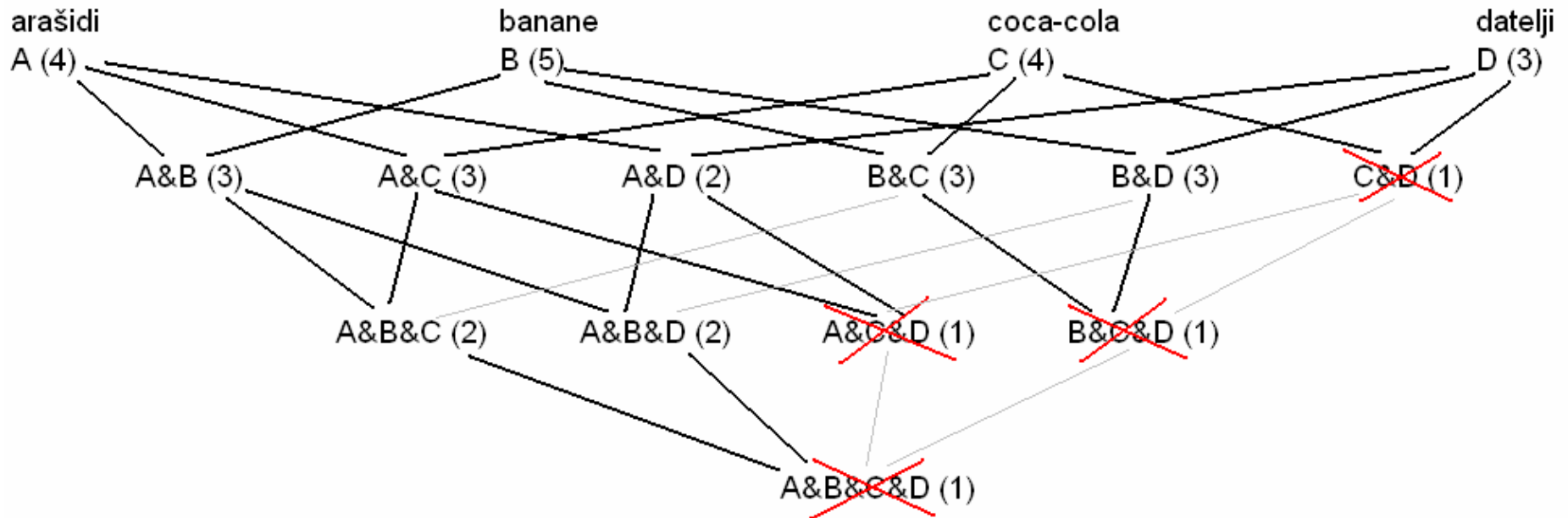
Frequent itemsets algorithm

Items in an itemset should be sorted alphabetically.

- Generate all 1-itemsets with the given minimum support.
- Use 1-itemsets to generate 2-itemsets with the given minimum support.
- From 2-itemsets generate 3-itemsets with the given minimum support as unions of 2-itemsets with the same item at the beginning.
- ...
- From n -itemsets generate $(n+1)$ -itemsets as unions of n -itemsets with the same $(n-1)$ items at the beginning.

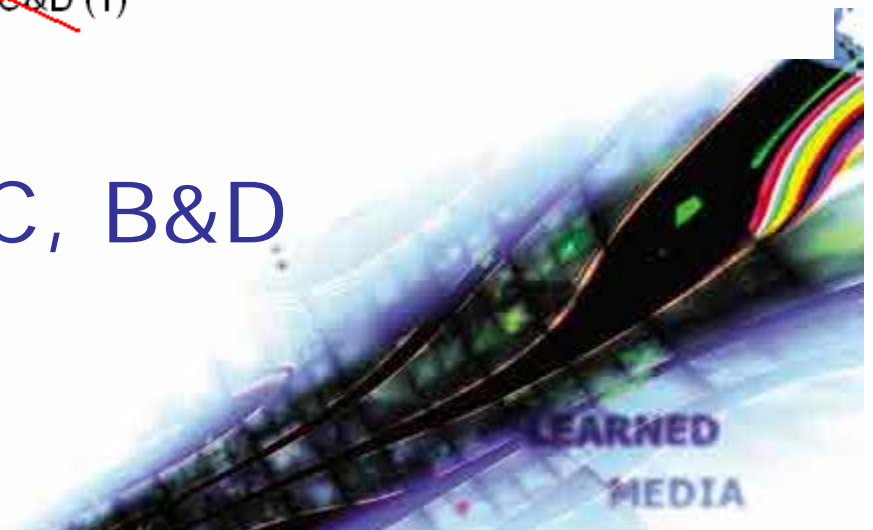


Frequent itemsets lattice



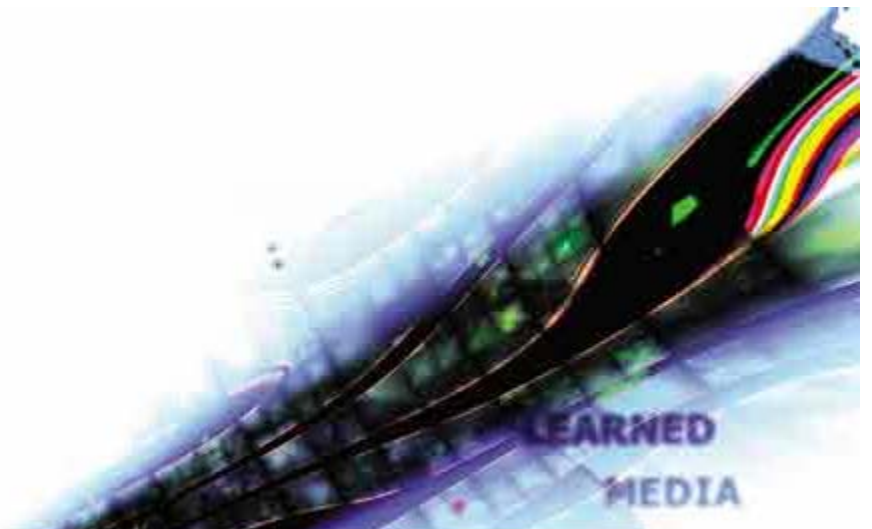
Frequent itemsets:

- A&B, A&C, A&D, B&C, B&D
- A&B&C, A&B&D



Rules from itemsets

- A&B is a frequent itemset with support 3/6
- Two possible rules
 - $A \rightarrow B$ confidence = $\#(A \& B) / \#A = 3/4$
 - $B \rightarrow A$ confidence = $\#(A \& B) / \#B = 3/5$
- All the counts are in the itemset lattice!



Discussion

- Transformation of an attribute-value dataset to a transaction dataset.
- What would be the association rules for a dataset with two items A and B, each of them with support 80% and appearing in the same transactions as rarely as possible?
 - minSupport = 50%, min conf = 70%
 - minSupport = 20%, min conf = 70%
- What if we had 4 items: A, $\neg A$, B, $\neg B$
- Compare decision trees and association rules regarding handling an attribute like "PersonID". What about attributes that have many values (eg. Month of year)

A	B
Green	White
Green	White
Green	Blue
Green	Blue
Green	Blue
Green	Blue
Green	Blue
Green	Blue
White	Blue
White	Blue

Quality of association rules

$$\text{Support}(X) = \#X / \#D \quad \dots\dots\dots P(X)$$

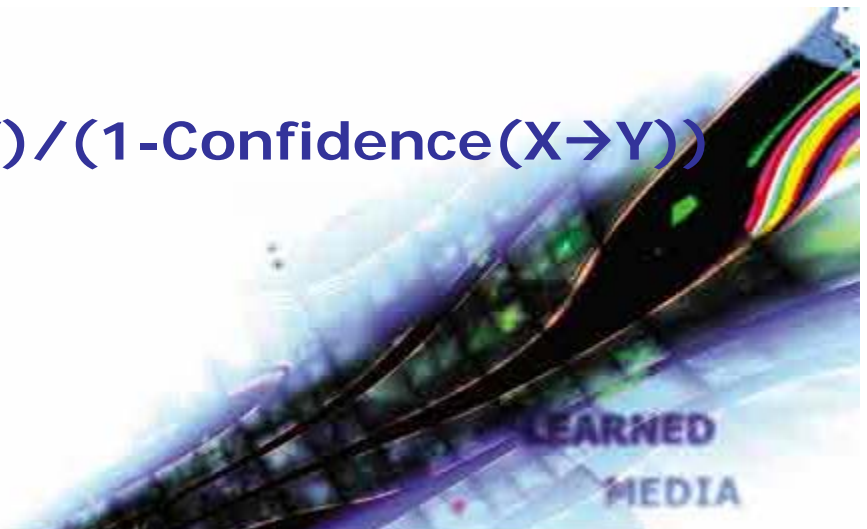
$$\text{Support}(X \rightarrow Y) = \text{Support}(XY) \#XY / \#D \quad \dots\dots\dots P(XY)$$

$$\text{Confidence}(X \rightarrow Y) = \#XY / \#X \quad \dots\dots\dots P(Y|X)$$

$$\text{Lift}(X \rightarrow Y) = \text{Support}(X \rightarrow Y) / (\text{Support}(X) * \text{Support}(Y))$$

$$\text{Leverage}(X \rightarrow Y) = \text{Support}(X \rightarrow Y) - \text{Support}(X) * \text{Support}(Y)$$

$$\text{Conviction}(X \rightarrow Y) = 1 - \text{Support}(Y) / (1 - \text{Confidence}(X \rightarrow Y))$$



Quality of association rules

$$\text{Support}(X) = \#X / \#D \quad \dots\dots\dots P(X)$$

$$\text{Support}(X \rightarrow Y) = \text{Support}(XY) \#XY / \#D \quad \dots\dots\dots P(XY)$$

$$\text{Confidence}(X \rightarrow Y) = \#XY / \#X \quad \dots\dots\dots P(Y|X)$$

$$\text{Lift}(X \rightarrow Y) = \text{Support}(X \rightarrow Y) / (\text{Support}(X) * \text{Support}(Y))$$

How many more times the items in X and Y occur together than it would be expected if the itemsets were statistically independent.

$$\text{Leverage}(X \rightarrow Y) = \text{Support}(X \rightarrow Y) - \text{Support}(X) * \text{Support}(Y)$$

Similar to lift, difference instead of ratio.

$$\text{Conviction}(X \rightarrow Y) = 1 - \text{Support}(Y) / (1 - \text{Confidence}(X \rightarrow Y))$$

Degree of implication of a rule.
Sensitive to rule direction.

