

Keywords	
Selection Data	
• Data	
<ul> <li>Attribute, example, attribute-v discretization</li> </ul>	value data, target variable, class,
Algorithms	
<ul> <li>Decision tree induction, entrop Occam's razor, model pruning association rules, support, con regression tree, model tree, h predictive vs. descriptive DM</li> </ul>	, naïve Bayes classifier, KNN,
Evaluation	
<ul> <li>Train set, test set, accuracy, c validation, true positives, false precision, recall</li> </ul>	
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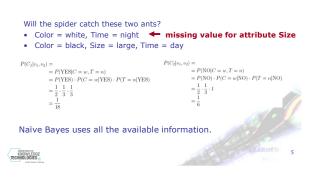
#### Discussion

- 1. Compare naïve Bayes and decision trees (similarities and differences).
  - 2. Compare cross validation and testing on a separate test set.
  - 3. Why do we prune decision trees?
  - 4. What is discretization.
  - 5. Why can't we always achieve 100% accuracy on the training set?
  - 6. Compare Laplace estimate with relative frequency.
  - 7. Why does Naïve Bayes work well (even if independence assumption is clearly violated)?
  - 8. What are the benefits of using Laplace estimate instead of relative frequency for probability estimation in Naïve Bayes?



# Comparison of naïve Bayes and decision

trees: Handling missing values



# Comparison of naïve Bayes and decision trees

- Similarities
  - Classification

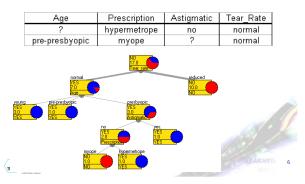
Kayuyanda

- Same evaluation
- Differences
  - Missing values
  - Numeric attributesInterpretability of the model
  - Model size



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# Comparison of naïve Bayes and decision trees: Handling missing values



Comparison of naïve Bayes and decision trees: Handling missing values

Algorithm **ID3**: does not handle missing values Algorithm C4.5 (J48) deals with two problems:

- Missing values in train data: - Missing values are not used in gain and entropy calculations
- Missing values in test data:
  - A missing continuous value is replaced with the median of the training set
  - A missing categorical values is replaced with the most frequent value

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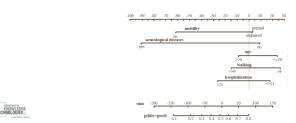
#### Comparison of naïve Bayes and decision trees: numeric attributes

- Decision trees ID3 algorithm: does not handle continuous attributes  $\rightarrow$  data need to be discretized
- Decision trees C4.5 (J48 in Weka) algorithm: deals with continuous attributes as shown earlier
- Naïve Bayes: does not handle continuous attributes  $\rightarrow$  data need to be discretized (some implementations do handle)



#### Comparison of naïve Bayes and decision trees: Interpretability

- Decision trees are easy to understand and interpret (if they are of moderate size)
- Naïve bayes models are of the "black box type".
- Naïve bayes models have been visualized by nomograms.



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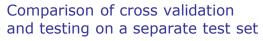
#### Comparison of naïve Bayes and decision trees: Model size

- Naïve Bayes model size is low and guite constant with respect to the data
- Trees, especially random forest tend to be very large









- · Both are methods for evaluating predictive models.
- Testing on a separate test set is simpler since we split the data into two sets: one for training and one for testing. We evaluate the model on the test data.
- Cross validation is more complex: It repeats testing on a separate test n times, each time taking 1/n of different data examples as test data. The evaluation measures are averaged over all testing sets therefore the results are more reliable.





# (Train – Validation – Test) Set

- Training set: a set of examples used for learning
- Validation set: a set of examples used to tune the parameters of a classifier
- Test set: a set of examples used only to assess the performance of a fully-trained classifier
- Why separate test and validation sets? The error rate estimate of the final model on validation data will be biased (optimistic compared to the true error rate) since the validation set is used to select the final model. After assessing the final model on the test set, YOU MUST NOT tune the model any further!





Decision tree pruning

- To avoid overfitting
- Reduce size of a model and therefore increase understandability.



#### Discretization

- A good choice of intervals for discretizing your continuous feature is key to improving the predictive performance of your model.
- Hand-picked intervals good knowledge about the data
- · Equal-width intervals probably won't give good results
- Find the right intervals using existing data:
  - Equal frequency intervals
  - If you have labeled data, another common technique is to find the intervals which maximize the information gain
  - Caution: The decision about the intervals should be done based on training data only

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 Global (before building the model) and local (during model construction on a subset at hand) discretization

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# Why can't we always achieve 100% accuracy on the training set?

- Two examples have the same attribute values but different classes (noisy data)
- Run out of attributes



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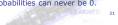
#### Relative frequency vs. Laplace estimate

#### **Relative frequency**

- P(c) = n(c) /N
   A disadvantage of using relative frequencies for probability estimation arises with small sample sizes, especially if they are either very close to zero, or very close to one.
- In our spider example: P(Time=day|caught=NO) = = 0/3 = 0
- n(c) ... number of examples where c is true N ... number of all examples k ... number of possible events

#### Laplace estimate

- Assumes uniform prior distribution over the probabilities for each possible event
- P(c) = (n(c) + 1) / (N + k)
   In our spider example: P(Time=day|caught=NO) =
- (0+1)/(3+2) = 1/5 With lots of evidence
- approximates relative frequency If there were 300 cases when the spider didn't catch ants at night: P(Time=day|caught=NO) =(0+1)/(300+2) = 1/302 = 0.003
- With Laplace estimate probabilities can never be 0.



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Discussion

differences)

training set?

Bayes?

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Compare naïve Bayes and decision trees (similarities and

Compare cross validation and testing on a separate test

Why can't we always achieve 100% accuracy on the

Compare Laplace estimate with relative frequency.

Why does Naïve Bayes work well (even if independence

What are the benefits of using Laplace estimate instead of relative frequency for probability estimation in Naïve

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#### Why does Naïve Bayes work well?



Because classification doesn't require accurate probability estimates as long as maximum probability is assigned to the correct class.



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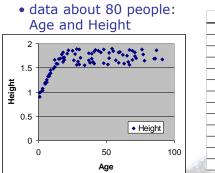
#### Benefits of Laplace estimate

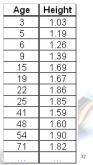
- With Laplace estimate we avoid assigning a probability of 0, as it denotes an impossible event
- $\bullet\,$  Instead we assume uniform prior distribution of k classes

#### Numeric prediction



#### Example





#### Test set

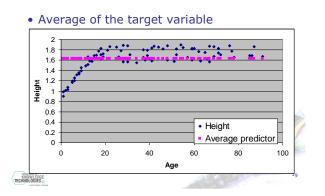
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Age	Height
2	0.85
10	1.4
35	1.7
70	1.6



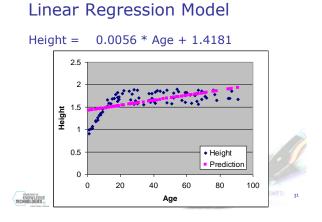
# Baseline numeric predictor



# Baseline predictor: prediction

#### Average of the target variable is 1.63

	Age	Height	Baseline	
	2	0.85		
	10	1.4		
	35	1.7		
	70	1.6		6. V
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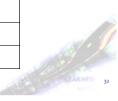


#### Linear Regression: prediction

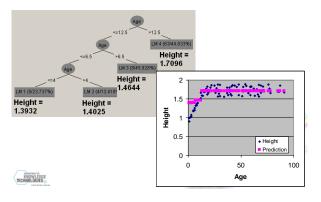
Height = 0.0056 \* Age + 1.4181

		Linear
Age	Height	regression
2	0.85	
10	1.4	
35	1.7	
70	1.6	

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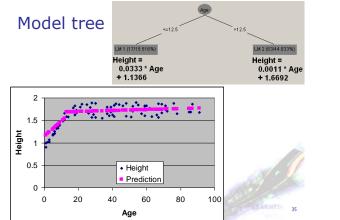


#### Regression tree

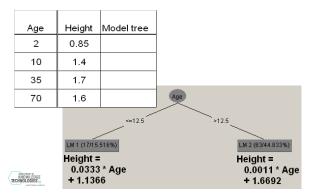


# Regression tree: prediction

400 est	Age >6.5 LM 3 (8/45.926 Height =	<pre>&gt;12.5 LM 4 (63/44.833%) Height = 1.7096</pre>		
LM 1 (5/23.737%)	2 (4/13.419)			Regression
Height = Hei	ight =	Age	Height	tree
1.3932 1.4	025	2	0.85	
		10	1.4	
		35	1.7	
		70	1.6	

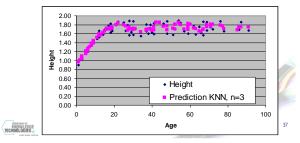


### Model tree: prediction



#### KNN – K nearest neighbors

- Looks at K closest examples (by non-target attributes) and predicts the average of their target variable
- In this example, K=3



#### **KNN** prediction



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#### KNN prediction

Age	Height	
8	1.36	
8	1.33	
9	1.45	
9	1.39	
11	1.49	
12	1.66	
12	1.52	
13	1.59	
14	1.58	
		-

			1
Age	Height	kNN	
2	0.85		
10	1.4		
35	1.7		1
70	1.6		
			39

### KNN prediction

	Age	Height	
	30	1.57	_
	30	1.88	
	31	1.71	_
	34	1.55	
	37	1.65	
	37	1.80	_
	38	1.60	
	39	1.69	
	39	1.80	
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Age	Height	kNN	
2	0.85		
10	1.4		
35	1.7		4
70	1.6		1
			40

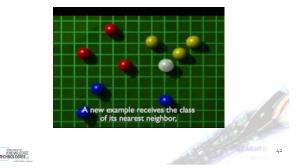
#### **KNN** prediction

Age	Height
67	1.56
67	1.87
69	1.67
69	1.86
71	1.74
71	1.82
72	1.70
76	1.88



# KNN video

<u>http://videolectures.net/aaai07\_bosch\_knnc</u>



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Age	Height	Baseline	Linear regression	Regressi on tree	Model tree	kNN
2	0.85	1.63	1.43	1.39	1.20	1.00
10	1.4	1.63	1.47	1.46	1.47	1.44
35	1.7	1.63	1.61	1.71	1.71	1.67
70	1.6	1.63	1.81	1.71	1.75	1.77

Which predictor is the best?



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n Target variable: Categorical (nominal) parate test set, Error: 1-accuracy
Categorical (nominal) parate test set, Error:
parate test set, Error:
Error:
1-accuracy
Algorithms:
Decision trees, Naïve Bayes,
Baseline predictor:
Majority class

#### Association rules

- Rules  $X \rightarrow Y$ , X, Y conjunction of items
- Task: Find **all** association rules that satisfy minimum support and minimum confidence constraints
- Support:  $Sup(X \rightarrow Y) = #XY/#D \cong p(XY)$
- Confidence:  $Conf(X \rightarrow Y) = \#XY/\#X \cong p(XY)/p(X) = p(Y|X)$



- Association rules algorithm
- 1. Generate frequent itemsets with a minimum support constraint
- 2. Generate rules from frequent itemsets with a minimum confidence constraint
- \* Data are in a transaction database



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#### Evaluating numeric prediction

Performance measure	Formula
mean-squared error	$\frac{\left(p_1-a_1\right)^2+\ldots+\left(p_n-a_n\right)^2}{n}$
root mean-squared error	$\sqrt{\frac{\left(p_1-a_1\right)^2+\ldots+\left(p_n-a_n\right)^2}{n}}$
mean absolute error	$\frac{ p_1-a_1 +\ldots+ p_n-a_n }{n}$
relative squared error	$\frac{(p_1-a_1)^2+\ldots+(p_n-a_n)^2}{(a_1-\overline{a})^2+\ldots+(a_n-\overline{a})^2}, \text{ where } \overline{a} = \frac{1}{n}\sum_i a_i$
root relative squared error	$\sqrt{\frac{(p_1 - a_1)^2 + \ldots + (p_n - a_n)^2}{(a_1 - \overline{a})^2 + \ldots + (a_n - \overline{a})^2}}$
relative absolute error	$\frac{ p_1 - a_1  + \ldots +  p_n - a_n }{ a_1 - \overline{a}  + \ldots +  a_n - \overline{a} }$
correlation coefficient	$\frac{S_{PA}}{\sqrt{S_P S_A}}, \text{ where } S_{PA} = \frac{\sum_i (p_i - \overline{p})(a_i - \overline{a})}{n - 1},$
	$S_p = \frac{\sum_i (p_i - \overline{p})^2}{n-1}$ , and $S_A = \frac{\sum_i (a_i - \overline{a})^2}{n-1}$

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Association Rules

#### Association rules – transaction database

#### Items: **A**=apple, **B**=banana,

C=coca-cola, D=doughnut

- Client 1 bought: A, B, C, D
- Client 2 bought: B, C
- Client 3 bought: B, D
- Client 4 bought: A, C
- Client 5 bought: A, B, D
- Client 6 bought: A, B, C

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#### Frequent itemsets

 Generate frequent itemsets with support at least 2/6

Α	В	С	D		
1	1	1	1		
	1	1			
	1		1		
1		1			
1	1		1		
1	1	1			



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#### Frequent itemsets algorithm

Items in an itemset should be **sorted** alphabetically.

- 1. Generate all 1-itemsets with the given minimum support.
- Use 1-itemsets to generate 2-itemsets with the given minimum support.
- From 2-itemsets generate 3-itemsets with the given minimum support as unions of 2-itemsets with the same item at the beginning.
- 4. ...

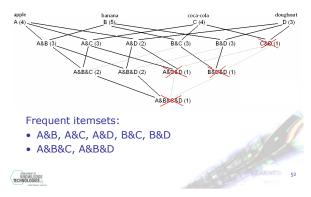
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- From n-itemsets generate (n+1)-itemsets as unions of nitemsets with the same (n-1) items at the beginning.
- To generate itemsets at level n+1 items from level n are used with a constraint: itemsets have to start with the same n-1 items.



HICOLO

# Frequent itemsets lattice



### Rules from itemsets

- A&B is a frequent itemset with support 3/6
- Two possible rules
  - A→B confidence = #(A&B)/#A = 3/4
  - B→A confidence = #(A&B)/#B = 3/5
- All the counts are in the itemset lattice!



### Quality of association rules

Support(X) = #X / #D	P(X)
Support(X $\rightarrow$ Y) = Support (XY)	= #XY / #D P(XY)
Confidence( $X \rightarrow Y$ ) = $\#XY / \#X$	P(Y X)

Lift( $X \rightarrow Y$ ) = Support( $X \rightarrow Y$ ) / (Support (X)\*Support(Y))

Leverage( $X \rightarrow Y$ ) = Support( $X \rightarrow Y$ ) - Support(X)\*Support(Y)

 $Conviction(X \rightarrow Y) = 1$ -Support(Y)/(1-Confidence(X \rightarrow Y))

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#### Next week



Scikit-learn is a free software machine learning library for the <u>Python</u> programming language. It features various <u>classification</u>, <u>regression</u> and <u>clustering</u> algorithms, and is designed to interoperate with the Python numerical and scientific libraries NumPy and SciPy.

#### • Install:

- Python 3
- NumPy
- Pandas
- Scikit-learn
- Recommended IDE: PyCharm Community

#### KNOWLEDGE

learn

# Discussion - part 2

- Transformation of an attribute-value dataset to a transaction dataset.
- What are the benefits of a transaction dataset?
- What would be the association rules for a dataset with two items A and B, each of them with support 80% and appearing in the same transactions as rarely as possible?
  - minSupport = 50%, min conf = 70%
     minSupport = 20%, min conf = 70%
- What if we had 4 items: A, ¬A, B, ¬ B
- Compare decision trees and association rules regarding handling an attribute like "PersonID". What about attributes that have many values (eg. Month of year)





#### Discussion - part 1

- 1. Can KNN be used for classification tasks?
- 2. Compare KNN and Naïve Bayes.
- 3. Compare decision trees and regression trees.
- 4. Consider a dataset with a target variable with five possible values:
  - non sufficient
     sufficient
  - 3. good 4. very good 5. excellent

  - 1. Is this a classification or a numeric prediction problem?
  - 2. What if such a variable is an attribute, is it nominal or numeric?

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