

## Decision Analysis Part 2: Decision Trees

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## Working Example

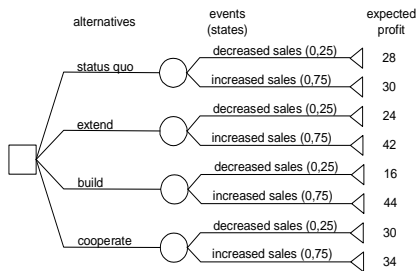
Decision table (Payoff matrix)

		alternative			
		status quo	extend	build	cooperate
states	decreased sales	28	24	16	30
	increased sales	30	42	44	34

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## Working Example

Equivalent *decision tree*:



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## Decision Tree

Different from decision trees used in Machine Learning:

- different types of nodes
- always drawn horizontally, from left to right
- "hand-crafted", not learned from data

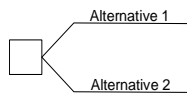
Decision tree represents the decision problem in terms of chains of consecutive *decisions* and chance *events*.

*Time* proceeds from *left to right*.

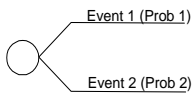
*Uncertainties* associated with chance events are modelled by *probabilities*.

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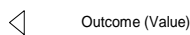
## Components of Decision Trees



**Decision node:**  
represents alternatives



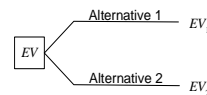
**Chance Node:**  
represents events (states of nature)



**Terminal (End) Node:**  
represents consequences of decisions

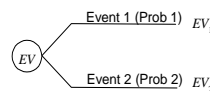
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## Solving Decision Trees

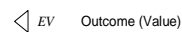


From right to left:

$EV = \max_i EV_i$  [maximize profit]  
or  
 $EV = \min_i EV_i$  [minimise losses]



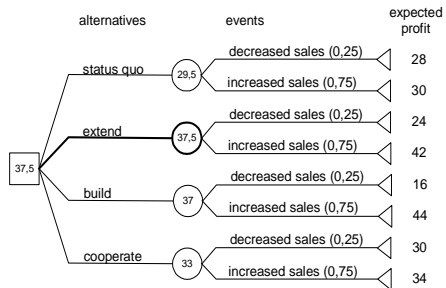
$EV = \sum_i p_i EV_i$



$EV = \text{Value}$

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## Solved Decision Tree



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## Decision Tree Development

1. Place decision and chance nodes in a logical time order
2. Independent chance nodes can be placed in any order
3. Estimate probabilities of all chance events
4. The sum of probabilities in a chance node must be 1
5. In terminal nodes, specify consequences by a single performance measure, e.g.:
  - money,
  - aggregate utility or
  - results of a multiple criteria analysis

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## Common Mistakes

1. Decision and chance nodes are in wrong order:  
Only chance nodes whose results are known at the time of decision can precede a decision node
2. Incorrect derivation of chance probabilities:  
Chance probabilities depend on each other and decisions made
3. Chance events with probability 0 can be left out
4. When solving the tree:  
Maximising instead of minimising, or vice versa

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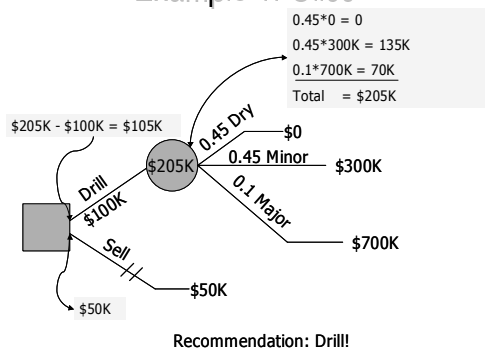
## Example 1: Oilco

Mobon Oil Company has a lease on an offshore oil site. The lease is about to expire and they are faced with either developing the field or selling the lease to Excel Oil Co. for \$50,000. It costs approximately \$100,000 to drill a well. There is a 45% chance that the well is dry, a 45% chance that the well will have a minor strike and a 10% chance that they will have a major strike. For a typical minor strike the revenues average \$300,000. If the strike is major the revenues average \$700,000. What should Mobon do?

Source: <http://www.cs.jmu.edu/common/courses/docs/sets411/Decision%20analysis%20lecture2a.ppt>

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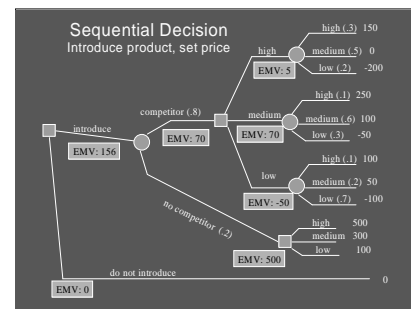
## Example 1: Oilco



Source: <http://www.cs.jmu.edu/common/courses/docs/sets411/Decision%20analysis%20lecture2a.ppt>

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## Example 2: Sequential Decision



Source: Decision Trees, [http://ocw.demic.udatn.edu/CharlesEbeling/MSC%20535/Lectures/Lesson%202/Decision\\_Tree%20decision%20trees.ppt](http://ocw.demic.udatn.edu/CharlesEbeling/MSC%20535/Lectures/Lesson%202/Decision_Tree%20decision%20trees.ppt)

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## Other Important Concepts

1. Value of Perfect Information
2. Risk Profile

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## Value of Perfect Information

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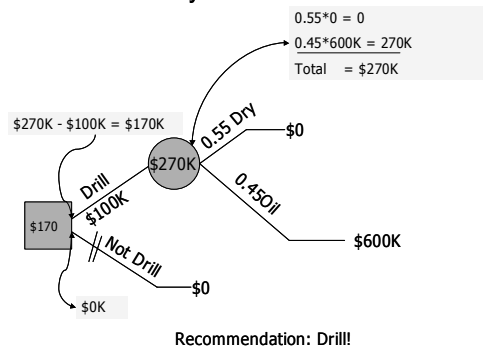
## Example

- Oilco must determine whether or not to drill for oil in the South China Sea. It costs \$100,000 to drill for oil and if oil is found the value of the oil is estimated to be \$600,000. At present, Oilco believes there is a 45% chance that the field contains oil. What should Oilco do?
- What is the *value of perfect information* (knowledge of whether the field contains oil) to Oilco?

Source: <http://www.cs.jmu.edu/oommon/courses/docs/issat11/Decision%20analysis%20lecture2a.ppt>

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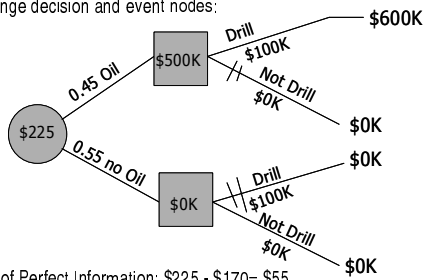
## Ordinary Decision Tree



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## Value of Perfect Information

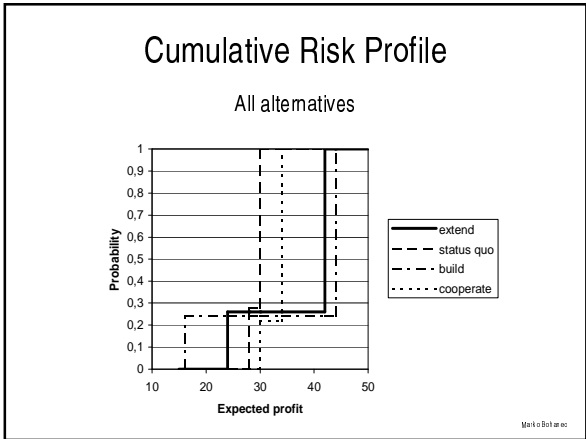
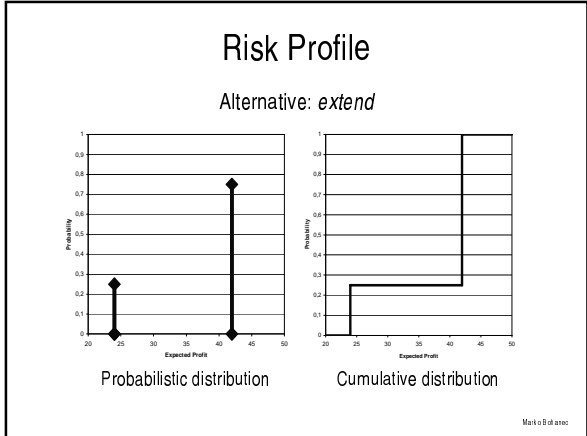
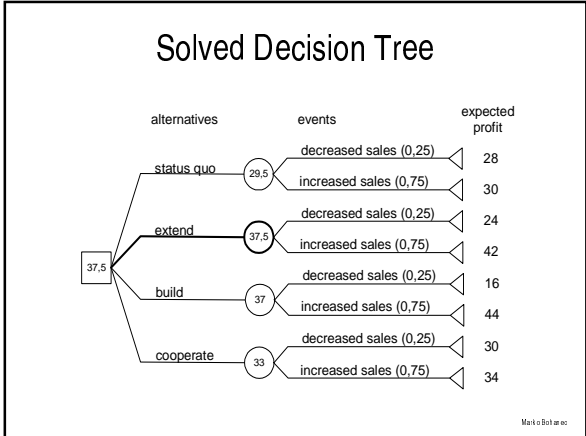
Exchange decision and event nodes:



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## Risk Profile



### Decision Tree Software

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### Decision Analysis Software

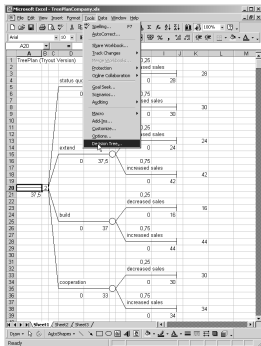
<http://decision-analysis.society.informs.org/Field/FieldSoftware.html>

See also:  
*OR/MS Today*, December 2006  
<http://www.lionhrpub.com/orms/surveys/das/das.html>

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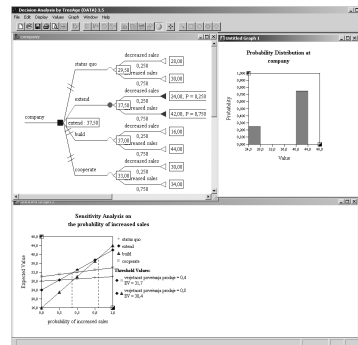
- ### Decision Tree Software
- Add-Ins for Microsoft Excel:**
- TreePlan: <http://www.treeplan.com/>
  - PrecisionTree: <http://www.palisade-europe.com/precisiontree/>
- Decision-Tree Development Programs:**
- TreeAge Pro (DATA): <http://www.treeage.com/>
  - DecisionPro: <http://www.vanguardsw.com/>
  - DPL: <http://www.syncopationsoftware.com/>
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## TreePlan



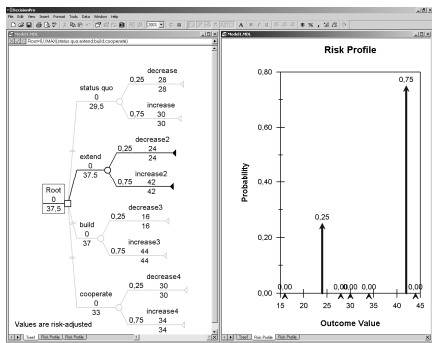
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## DATA



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## DecisionPro



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## A Typical Application in Medicine A Cost-Benefit Analysis of Testing for Influenza A in High-Risk Adults

William J. Heston, MD  
Joseph J. Benich III  
Department of Family Medicine, Medical  
University of South Carolina, Charleston, SC

**ABSTRACT**  
**BACKGROUND:** Clinical diagnosis and empiric therapy have been strategies for treatment of suspected influenza in high-risk patients, but rapid tests for influenza have been introduced to help confirm cases. The aim of this study was to determine when rapid testing, empiric treatment, or no treatment is most cost-beneficial for high-risk adults with influenza-like respiratory tract illnesses.

**METHODS:** We performed a cost-benefit analysis evaluating the comparative advantage of the strategies of empiric therapy, no treatment, or test and treat patients whose tests are positive. The analysis focused on a hypothetical population of patients who are at a high-risk for complications of influenza. Our main outcome was the cost of care for an episode of influenza idem from the human capital perspective.

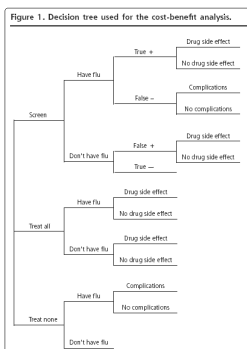
**RESULTS:** For older anti-influenza drugs (amantadine and rimantadine), rapid testing is not as cost-beneficial as empiric treatment, even when the prevalence of influenza is low. For the neuraminidase inhibitors, there is a narrow window of disease prevalence between 30% and 40% where testing is most cost-beneficial. When the disease likelihood is above this window, empiric treatment is preferred. Below this window, no treatment is more cost-beneficial. Even under the most favorable conditions, testing is preferred only for a small range of prevalence rates of influenza.

**CONCLUSION:** When clinicians are planning to use the nonneuraminidase inhibitors to treat influenza, rapid testing is not the most cost-beneficial approach. Even when the more expensive neuraminidase inhibitors will be used, testing has a limited role in managing influenza in high-risk patients.

Am Fam Med 2004;2:33-40. DOI: 10.1370/afm.34

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## A Typical Application in Medicine



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## Questions

Compare decision tables with decision trees:  
What do decision trees facilitate that decision tables don't?

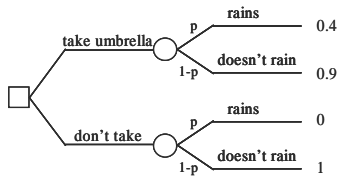
Identify limitations and/or shortcomings of decision trees.

Identify types of decision problems suitable for the application of decision trees.

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## Exercise 1

Consider the decision tree:



1. Solve the tree for tomorrow's  $p$
2. Do sensitivity analysis
3. Take the risk profile of your decision

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## Exercise 2

For the decision tree shown in the slide  
"Example 2: Sequential Decision" (Introduce Product):

1. do sensitivity analysis with respect to  $p(\text{competitor})$
2. find the risk profile of alternative *introduce*.

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## Tree Development Exercise (1/3)

### Service station problem:

- You are the owner of a service station on an intercity road. You have heard a rumour that the road may be upgraded or diverted along a different route. What do you do? What information will you need? How do you formulate a decision model?
- Think: before reading next slides, structure your own decision. You will need to specify an *objective*, identify *alternatives* available to you as the service station owner, and identify the *uncertainties* involved in this decision situation together with the possible *events*.

Adapted from: Making Decisions, <http://www.imm.ese.l.uwa.edu.au/unit450231/lectures/week%202.ppt>

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## Tree Development Exercise (2/3)

### Possible answers to the questions from the previous slide:

**Objective:** maximise the value of service station investment

### Alternatives:

- *status quo*
- *sell*
- *extend*

### Events:

- *unaltered* ( $p=0.5$ )
- *upgrade* ( $p=0.3$ )
- *divert* ( $p=0.2$ )

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## Tree Development Exercise (3/3)

### Proceed as follows:

1. Define decision table (include *consequences*)
2. Convert decision table to decision tree
3. Calculate *EV* and identify the best alternative
4. Do sensitivity analysis with respect to  $p(\text{unaltered})$   
[which problem do you encounter here?]
5. Find the risk profile of the best alternative

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