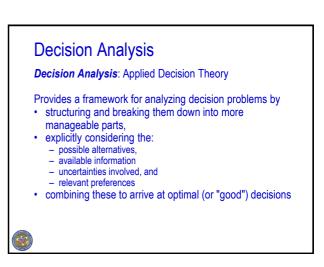
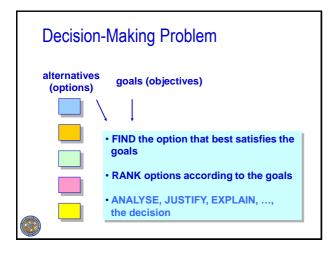
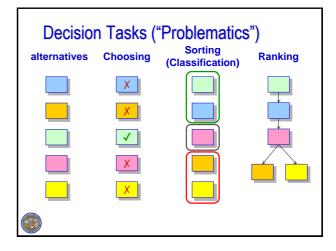


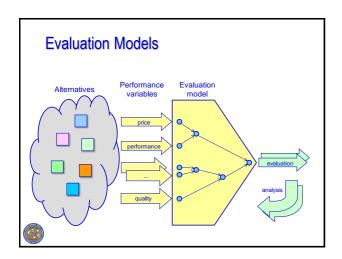
Decision Analysis
Part 1
Decision Analysis and Decision Tables

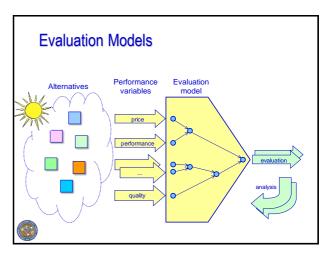
Decision Analysis, Part 1 Introduction to Decision Analysis Concepts: modelling, evaluation, analysis Decision Problem-Solving: Stages Relation of DA to some other Disciplines Decision-Making under Uncertainty Decision-Making under Strict Uncertainty Decision Table Various Decision Criteria Decision-Making under Risk Expected Value Sensitivity Analysis

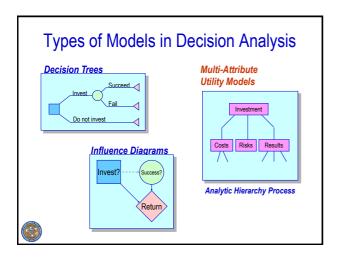


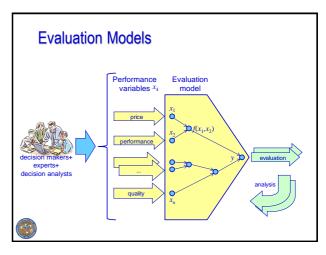


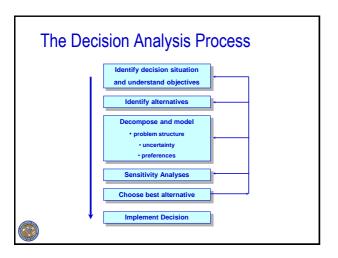


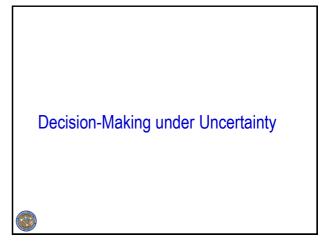












Decision-Making Problem

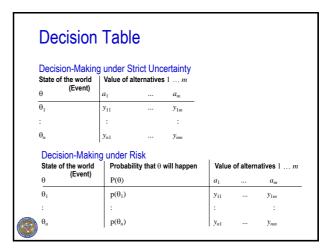
Suppose that one must choose between several *uncertain alternatives*.

Given:

- · Alternatives;
- The consequences of choosing each alternative, described with a single number,
 e.g. profit / loss in € or aggregated value.

Task: Which alternative to choose?





Working Example

A manufacturing company, faced with a possible increase in demand for its product, considers the following:

Alternatives:

- 1. status quo: no change
- 2. *extend*: extending their production line buying a new machine
- 3. *build*: building a new production hall with new equipment
- 4. cooperate: finding additional business parters for production

Uncertainty involved:

Market reaction: after the decision, the sales can increase or decrease.

Consequences:

Expected profit, shown in decision table on the next slide



Decision-Making under Strict Uncertainty



Decision Criteria

- Dominance
- · Pessimistic (Maximin, Wald's)
- · Optimistic (Maximax)
- Hurwicz's
- Laplace's
- Minimax Regret



Dominance

- Choose the alternative with best consequences in all states of the world.
- · Such alternative is seldom found.

			alten	native	
		status quo	extend	build	cooperate
states	decreased sales	28	24	16	30
sta	increased sales	30	42	44	34

No dominant alternatives in this case



Pessimistic Criterion (Wald's, Maximin)

- Each alternative is represented by its worst possible consequence.
- According to these, the alternative with the best worst case is chosen.

		alternative			
		status quo	extend	build	cooperate
states	decreased sales	28	24	16	30
sta	increased sales	30	42	44	34
Pess	imist	28	24	16	30



Optimistic Criterion (Maximax)

- Each alternative is represented by its best possible consequence.
- The alternative for which this best consequence is best is chosen.

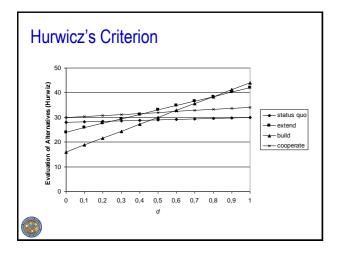
		alternative			
		status quo	extend	build	cooperate
states	decreased sales	28	24	16	30
sta	increased sales	30	42	44	34
Optin	nist	30	42	<u>44</u>	34



Hurwicz's Criterion

- Introduce a parameter $d \in [0,1]$.
- Combine Optimistic and Pessimistic criteria so that $u_h = du_o + (1-d)u_p$

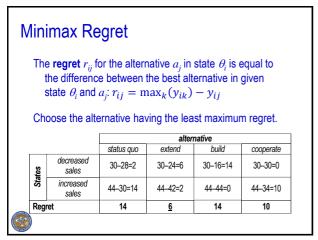
		alten	native	
	status quo	extend	build	cooperate
decreased sales	28	24	16	30
increased sales	30	42	44	34
simist	28	24	16	<u>30</u>
mist	30	42	<u>44</u>	34
viz (d=0,3)	28,6	29,4	24,4	<u>31,2</u>
	sales increased sales simist mist	decreased 28	status quo extend decreased sales 28 24 increased sales 30 42 simist 28 24 mist 30 42	decreased sales 28 24 16 increased sales 30 42 44 simist 28 24 16 mist 30 42 44



Laplace's Criterion

- · Consider all states (events) equally likely,
- thus, consider the *average* of outcomes for each alternative.

		alternative			
		status quo	extend	build	cooperate
states	decreased sales	28	24	16	30
sta	increased sales	30	42	44	34
Lapla	ace	29	<u>33</u>	30	32



Summary status quo decreased 24 30 28 16 increased 30 42 44 34 sales Pessimist 28 24 16 <u>30</u> Optimist 30 42 34 44 28,6 29,4 24,4 Hurwiz (d=0,3) 31,2 Laplace 29 33 30 32 14 14 10 Regret

Questions

- If you were the manager, which alternative would you take? Why?
- Is this really the best alternative? Why? Under which circumstances it is best?
- What can you say about the status quo alternative? According to the analysis, when should be it taken, or should it be taken at all?



Questions

Assess the presented decision criteria:

- · Describe the prevalent characteristics of each criterion
- What do you think about the criteria:
 - Are they comprehensible?
 - Are they realistic?
 - Are they useful for practice?
 - Which is your favourite criterion?
- Is there a single "best" criterion? Which and why?



Decision-Making under Risk



Working Example

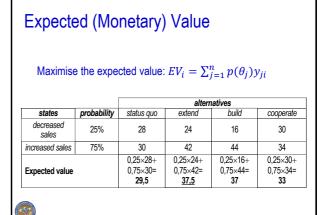
Now we know (or estimate) the probablity of states

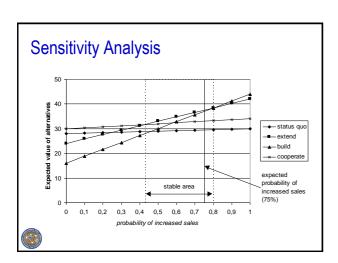
			alterr	atives	
states	probability	status quo	extend	build	cooperate
decreased sales	25%	28	24	16	30
increased sales	75%	30	42	44	34

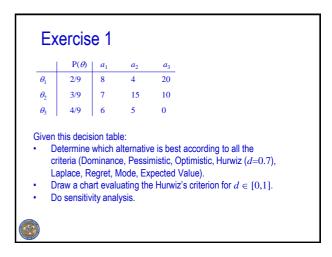


Decision Criteria

- · Mode: Select the most probable state
- Expected Value (EV), Expected Monetary Value (EMV)







Help the farmer wh the face of unc yield:	•		•
	We	ather	
probability	.55	.15	30
	Normal	Drought	Rainy
Plant soybeans	\$ 10	5	12
Plant corn	7	8	13
	' I	profit per acre	

Exercise 3

- 1. Define a decision problem of your own,
- 2. represent it in a decision table,
- 3. and repeat the steps of Exercise 1

Exercise 2

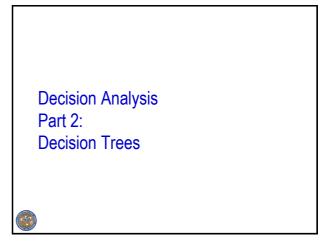
Exercise 4

Using some decision table, implement in spreadsheet software (such as MS Excel):

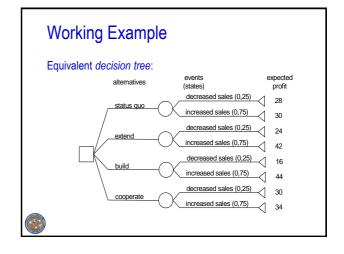
- · evaluation of alternatives using all the criteria,
- drawing the chart associated with Hurwiz's criterion
- · drawing the sensitivity analysis chart

Compare the two charts.

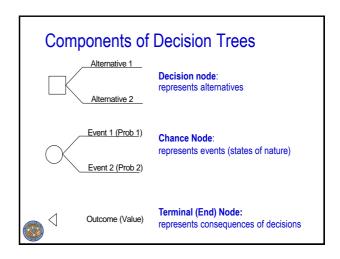


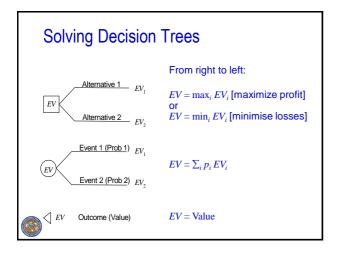


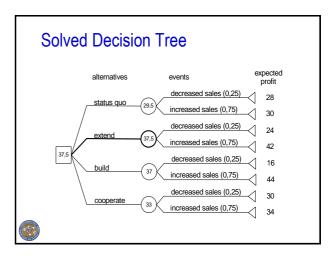
Working Example Decision table (Payoff matrix) | Sales | decreased | sales | sales | increased | sales | sal



Decision Tree Different from decision trees used in Machine Learning: different types of nodes always drawn horizontally, from left to right mand-crafted, not learned from data Decision tree represents the decision problem in terms of chains of consecutive decisions and chance events. Time proceeds from left to right. Uncertainties associated with chance events are modelled by probabilities.







Decision Tree Development

- 1. Place decision and chance nodes in a logical time order
- 2. Independent chance nodes can be placed in any order
- 3. Estimate probabilities of all chance events
- 4. The sum of probabilities in a chance node must be 1
- 5. In terminal nodes, specify consequences by a single performance measure, e.g.:
 - money.
 - aggregate utility or
 - results of a multiple criteria analysis



Common Mistakes

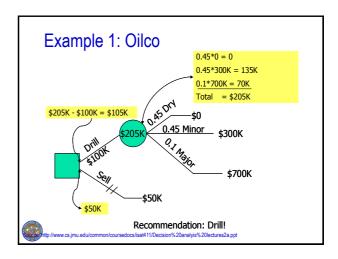
- Decision and chance nodes are in wrong order:
 Only chance nodes whose results are known at the time
 of decision can precede a decision node
- Incorrect derivation of chance probabilities:
 Chance probabilities depend on each other and decisions made
- 3. Chance events with probability 0 can be left out
- When solving the tree: Maximising instead of minimising, or vice versa

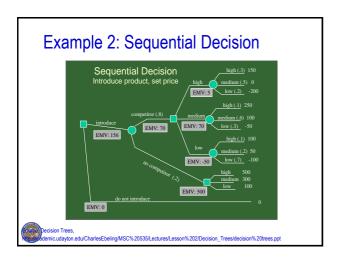


Example 1: Oilco

Mobon Oil Company has a lease on an offshore oil site. The lease is about to expire and they are faced with either developing the field or selling the lease to Excel Oil Co. for \$50,000. It costs approximately \$100,000 to drill a well. There is a 45% chance that the well is dry, a 45% chance that the well will have a minor strike and a 10% chance that they will have a major strike. For a typical minor strike the revenues average \$300,000. If the strike is major the revenues average \$700,000. What should Mobon do?



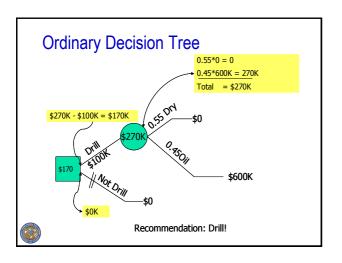


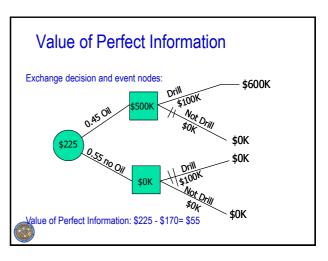


Other Important Concepts 1. Value of Perfect Information 2. Risk Profile

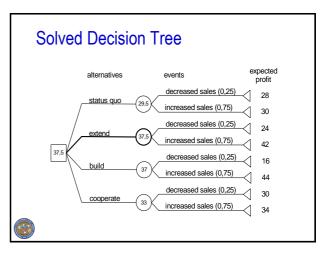
Value of Perfect Information

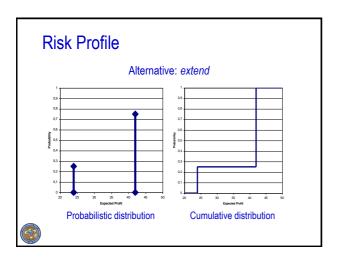
Oilco must determine whether of not to drill for oil in the South China Sea. It costs \$100,000 to drill for oil and if oil is found the value of the oil is estimated to be \$600,000. At present, Oilco believes there is a 45% chance that the field contains oil. What should Oilco do? What is the value of perfect information (knowledge of whether the field contains oil) to Oilco?

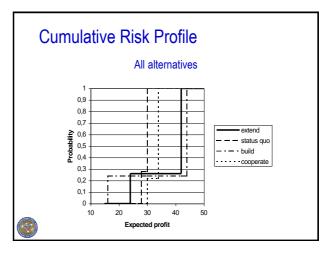




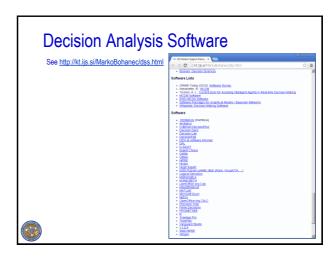




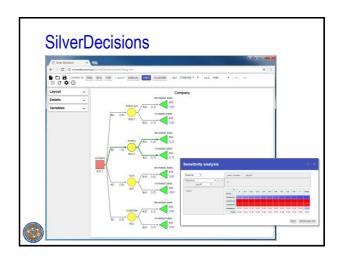


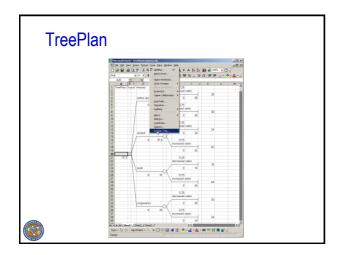


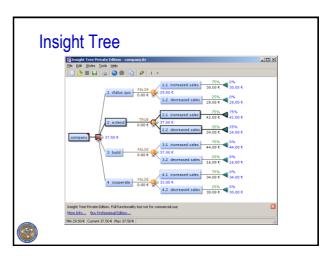
Decision Tree Software

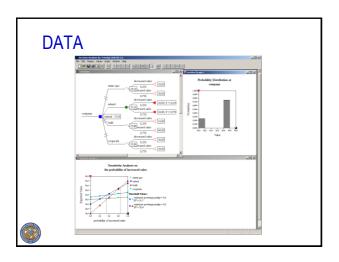


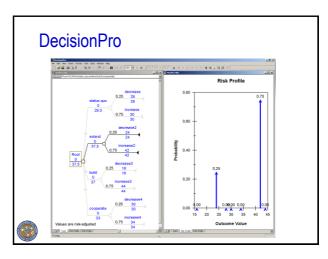


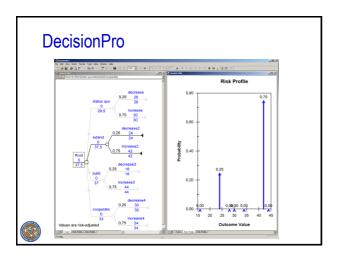




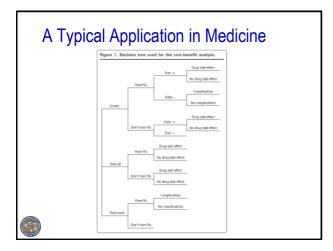




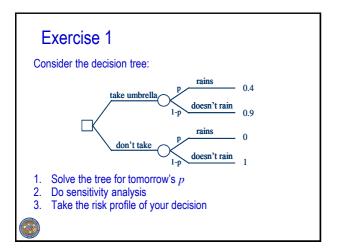




A Typical Application in Medicine A Cost-Benefit Analysis of Testing for Influenza A in High-Risk Adults William J. Hurster, MD Joseph J. Rench III Department of Fash Moders, Model Department of Fash Moders, Model Department of South Candons, Chadeson, SC Influenzation of South Candons, Chadeson, SC METODO (South Candons, Chadeson, Sc MET



Questions Compare decision tables with decision trees: What do decision trees facilitate that decision tables don't? Identify limitations and/or shortcomings of decision trees. Identify types of decision problems suitable for the application of decision trees.



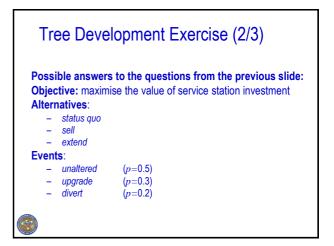
Exercise 2 For the decision tree shown in the slide "Example 2: Sequential Decision" (Introduce Product): 1. do sensitivity analysis with respect to p(competitor) 2. find the risk profile of alternative introduce.

Tree Development Exercise (1/3)

Service station problem:

- You are the owner of a service station on an intercity road. You have heard a rumour that the road may be upgraded or diverted along a different route. What do you do? What information will you need? How do you formulate a decision model?
- Think: before reading next slides, structure your own decision. You will need to specify an objective, identify alternatives available to you as the service station owner, and identify the uncertainties involved in this decision situation together with the possible events.

apted from: Making Decisions, http://www.imm.ecel.uwa.edu.au/unit450231/lectures/week%202.ppl



Tree Development Exercise (3/3)

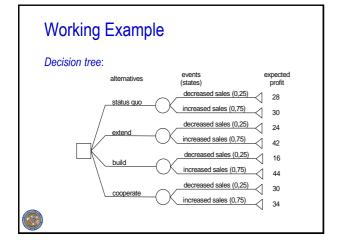
Proceed as follows:

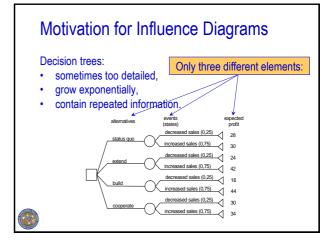
- 1. Define decision table (include consequences)
- 2. Convert decision table to decision tree
- 3. Calculate EV and identify the best alternative
- 4. Do sensitivity analysis with respect to *p*(*unaltered*) [which problem do you encounter here?]
- 5. Find the risk profile of the best alternative

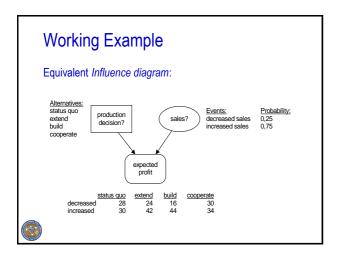


Decision Analysis
Part 3:
Influence Diagrams

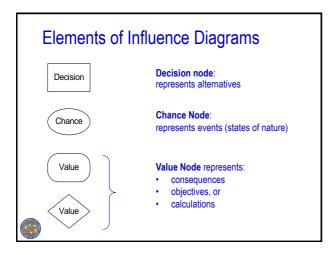


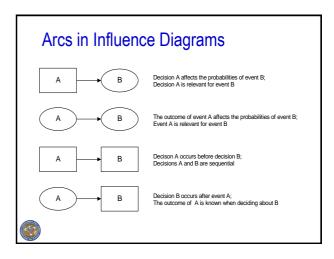






Influence Diagram Influence diagram is a: • high-level (compact), • visual representation, • displaying relationships between essential elements that affect the decision. Two levels of detail: • higher: only elements and relations • lower: detailed information defined with each element

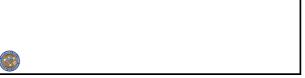




Developing Influence Diagrams

Two basic strategies:

- Start with outcomes and model towards decisions and events
- Gradually add more and more detail



Common Mistakes

- 1. An influence diagram is not a flowchart.
- An arc from a chance node into a decision node means that the decision-maker knows the outcome of the chance node when making the decision.
- 3. There can be no cycles:



Decision Trees: Influence Diagrams

- DT display more information, the details of a problem, but they may become "messy".
- ID show a general structure of a problem and hide details.
- ID are particularly valuable for the structuring phase of problem solving and for representing large problems.
- Solving algorithms: DT straightforward, ID difficult
- Any properly built ID can be converted into a DT, and vice versa.
- Bayesian networks are ID's containing only event nodes



Solving Influence Diagrams

- A. Convert ID to DT, solve DT
- or
- B. Solve directly by node reduction:
 - Cleanup: one consequence *C*, no cycles, transform calculation nodes to one-event chance nodes...
 - 2. Repeat until ID solved:
 - Reduce (calculate EV of) all chance nodes that directly precede C and do not precede any other node.
 - Reduce (calculate EV of) the decision node that directly precedes C
 and has as predeccessors all of the other direct predeccessors of C.
 - arc reversal where there are no nodes corresponding to 2.2



Influence Diagram Software

Add-Ins for Microsoft Excel:

PrecisionTree: http://www.palisade.com

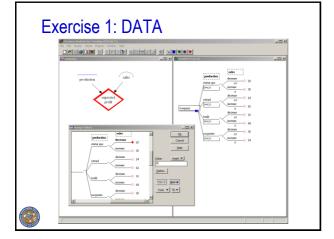
Influence-Diagram Development Programs:

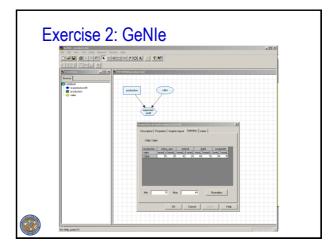
- GeNIe: https://dslpitt.org/genie/
- TreeAge Pro (DATA): http://www.treeage.com/
- DPL: https://www.syncopation.com
- Analytica: http://www.lumina.com/ana/whatisanalytica.htm
- HUGIN: http://www.hugin.com/
- Netica: http://www.norsys.com/

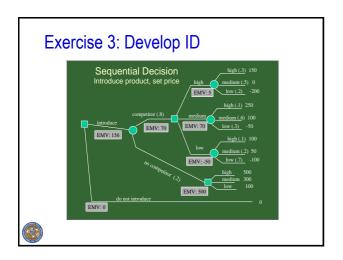


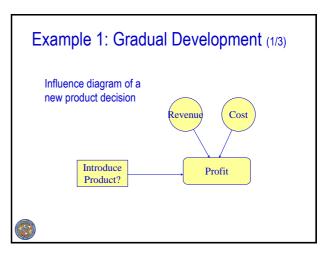
Exercises

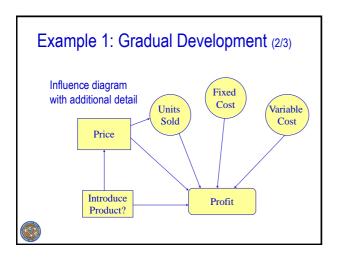


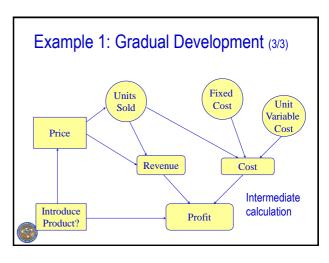


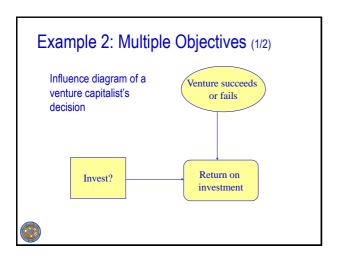


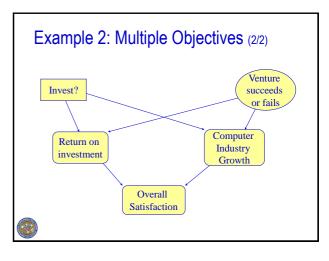


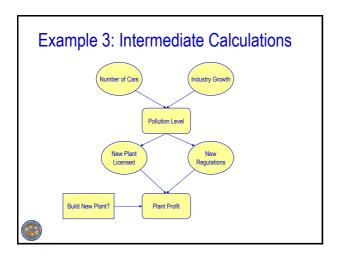


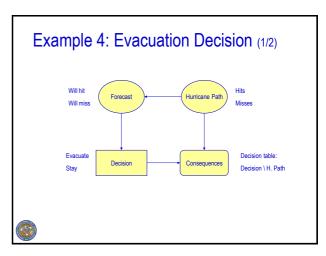


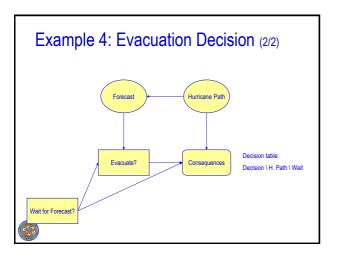


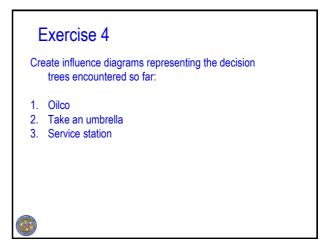






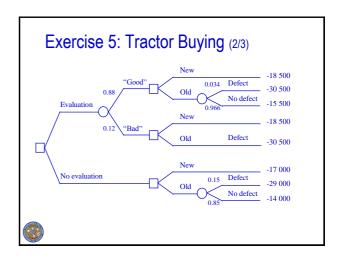






Your uncle is going to buy a tractor. He has two alternatives: 1. A new tractor (17 000 €) 2. An used tractor (14 000 €) The engine of the old tractor may be defect, which is hard to ascertain. Your uncle estimates a 15 % probability for the defect. If the engine is defect, he has to buy a new tractor and gets 2000 € for the old one. Before buying, your uncle can take the old tractor to a garage for an evaluation, which costs 1 500 €. If the engine is OK, the garage can confirm it without exception. If the engine is defect, there is a 20 % chance that the garage does not

Exercise 5: Tractor Buying (1/3)



Exercise 5: Tractor Buying (3/3)

Do the following:

- 1. Solve the decision tree
- 2. Develop equivalent influence diagram:
 - 1. structure of nodes
 - 2. detailed node data (names, values, probabilities)

