# Qualitative multi-attribute decision method DEX: Theory and practice

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# Outline

- Method DEX
  - Informal introduction
  - Formal representation of DEX models

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- Methods for development and exploitation of DEX models
- Software
- Applications

## What is DEX?

Decision Support, Multi-Attribute Modeling Methodology





## What is DEX?

# DEX

#### **Multi-Criteria Decision Analysis**

- modeling using criteria and utility functions
- problem decomposition and structuring
- evaluation and analysis of decision alternatives

#### Artificial Intelligence Expert Systems

- qualitative (symbolic) variables
- "if-then" rules
- decision model = knowledge base
- handling imprecision and uncertainty
- transparent models, explanation
   Machine Learning

#### **Fuzzy sets**

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- verbal measures
- fuzzy operators





### Multiattribute Decisionmaking Using a Fuzzy Heuristic Approach

JANET EFSTATHIOU AND VLADISLAV RAJKOVIČ

Abstract—Multiattribute decisionmaking (DM) is treated as a special kind of structured human problem solving. Emphasis is placed on the use of the available knowledge about utilities, which is obtained by combining beuristics and traditional aggregation methods. In this way, the problem of partial utilities and their interdependence may be solved. A fuzzy approach to DM is described, incorporating linguistic variables, relations, and algorithms. It is summarized in a formal model and illustrated by an example.



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## DEX

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### Method for qualitative multi-attribute modeling

DEX is similar to other multi-attribute methods:

- 1. Multiple attributes, hierarchically structured
- 2. Evaluation of alternatives: bottom-up aggregation



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### Method for <u>qualitative</u> multi-attribute modeling

DEX is different from the majority of multi-attribute methods:

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1. Attributes are discrete, symbolic, qualitative





## DEX

### Method for <u>qualitative</u> multi-attribute modeling

DEX is different from the majority of multi-attribute methods:

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 Attributes are discrete, symbolic, qualitative Attribute scales can be <u>unordered</u> (categorical), but are typically <u>preferentially ordered</u> (increasing or decreasing)







### Method for <u>qualitative</u> multi-attribute modeling

DEX is different from other multi-attribute methods:

2. Evaluation of alternatives (aggregation) is defined by *decision tables* 



Model: Attributes: Hierarchy:  $S: X \to 2^X$ 

M = (X, S, D, F) $X = \{x_1, x_2, \dots, x_n\}$ so that  $\forall x \in X : x \notin S^*(x)$ 

descendants of X no cycles





Model: Attributes: Hierarchy:

M = (X, S, D, F)es:  $X = \{x_1, x_2, \dots, x_n\}$ ny:  $S: X \to 2^X$ so that  $\forall x \in X: x \notin S^*(x)$ 

descendants of X no cycles





Model: Attributes: Hierarchy:

M = (X, S, D, F) $X = \{x_1, x_2, \dots, x_n\}$  $S: X \to 2^X$ so that  $\forall x \in X : x \notin S^*(x)$ 

descendants of X no cycles



Model: M = (X, S, D, F)Value scales:  $D = \{D_1, D_2, \dots, D_n\}$ for i = 1, 2, ..., n:  $x_i \in D_i$  $D_i = \{v_i^1, v_i^2, \dots, v_i^{d_i}\}, d_i > 1$ For an increasing  $D_i$ :  $v_i^j \leq_i v_i^{j+1}$ ,  $j = 1, 2, ..., d_i - 1$ For a decreasing  $D_i$ :  $v_i^{j+1} \leq_i v_i^j$ ,  $j = 1, 2, ..., d_i - 1$ Each  $D_i$  is partitioned into  $B_i$ ,  $N_i$ ,  $G_i$  so that  $D_i = B_i \cup N_i \cup G_i$  and  $B_i \leq N_i \leq G_i$ 



Model: M = (X, S, D, F)Utility (aggregation) functions:

 $F = \{F_i | x_i \text{ is aggregate}\}$  $F_i : \times_{s \in S(x_i)} \to E_i, \text{ total}$ 



Possible formulations of  $E_i$ :

"Basic":  $E_i \equiv D_i$ 

 $E_i \equiv D_i$ if SAFETY=good & COMFORT=med then TECH.=good

"Practical":  $E_i \equiv \text{interval over } D_i$ 

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if SAFETY=good & COMFORT=good then TECH=[good,exc] (or ≥good)

"Extended":  $E_i \equiv \text{distribution over } D_i \text{ (probabilistic, fuzzy)}$ if SAFETY=good & COMFORT=med then TECH=(good/0.7; exc/0.3)



# **DEX Method: Dynamic Aspects**

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#### How to:

- Obtain model and its components?
- Verify model and its components (e.g. for completeness and consistency)?
- Deal with uncertainty? •
- Ensure transparency, comprehensibility?
- Support model dynamics?

#### How to:

- Obtain and represent data about alternatives?
- Deal with incomplete, uncertain data?
- Explain and justify results?
- Validate results?
- Carry out the analyses? • Which analyses?
- Assess the quality of • decision?





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Preview

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#### **Functionality:**

- creation and editing of qualitative DEX models: •
  - model structure
  - decision tables
- acquisition and evaluation of alternatives •
- analysis of alternatives: "what-if", "±1 analysis", comparison of alternatives, selective explanation ٠
- tabular and graphical reports •

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Obtaining attributes, their value scales and model structure:

 Expert modeling, 'hand-crafting', following guidelines and 'rules of thumb'

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- Machine learning from data (methods: HINT, Model Revision)

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### Acquisition of decision tables and decision rules

- Active support
- Three "strategies":
  - Direct
  - 'Use scale orders' (based on dominance)
  - 'Use weights' (based on attributes' weights)
- Validation:
  - Consistency (based on dominance)
  - Completeness (% determined function values)

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- Principle:
  - 'The user is always right' (but warned if considered to be in error)

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#### Transparency: Representation and visualization of decision rules

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Aggregate rules



3D point-by-point graphic

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Bridging the gap between qualitative and quantitative value functions



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Handling changes of model structure and components:

- Adding, deleting, moving, connecting attributes and subtrees
- Adding, deleting, moving, joining attribute values

Principles:

- Preserve the available information as much as possible
- Perform operations 'behind the scene' (with due warnings)





Handling changes of model structure and components:

- Adding, deleting, moving, connecting attributes and subtrees
- Adding, deleting, moving, joining attribute values

#### Example: delete attribute value 'good' of CAR





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## **DEX Method: Model Exploitation**



### Evaluation of alternatives:

- Bottom-up table lookup
- Principle: Use all available information (even when data or rules are incomplete)
- Handling uncertainty:
  - interval/set values
  - probability distribution
  - fuzzy distributions

#### Missing data

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SAFETY	high	*

Scales: 1(

#### Missing decision table COMFORT

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Art of Modeling BARCELON Attributes: 10 (6 basic, 0 linked, 4 aggregate)

Attributes: 10 (6 basic, 0 linked, 4 aggregate) | Scales: 1(

## **DEX Method: Model Exploitation**



### Analysis of alternatives:

- "What-if analysis"
- "±1 analysis"

OR

- Compare alternatives
- Selective explanation

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# **DEX Milestones**

<ul> <li>Methodology</li> <li>initial development</li> <li>Software</li> <li>DECMAK</li> <li>"toolbag"</li> <li>First applications</li> <li>HW and SW selection</li> <li>personnel mgmt</li> <li>nursery schools</li> </ul>	<ul> <li>Methodology</li> <li>integration</li> <li>Software</li> <li>DEX</li> <li>Vredana</li> <li>National applications</li> <li>Housing Fund</li> <li>Ministry Sci-Tech</li> <li>Talent System</li> <li>industry</li> <li>medicine</li> <li>Related</li> <li>HINT</li> </ul>	Methodology • further improvement Software • DEXi Education International applications • Sol-Eu-Net • agronomy, GMO • project evaluation • finance Related • model revision, proDEX
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# **Evaluation of R&D Projects**

- Overall project evaluation
  - Contents evaluation
    - Evaluation of goals
    - Evaluation of objectives
  - Feasibility evaluation
    - Evaluation of external feasibility
    - Evaluation of internal feasibility
- Evaluation of goals
  - Direct benefits
    - Development benefits
      - Mastering of new technologies
      - Ecological impacts
      - Employment impacts
        - Employment generation
        - Impact on employment structure
    - Economic benefits
      - Impact on marketing
        - Opening of new markets
        - Anticipated share of export
        - Impact on decreasing imports
      - Anticipated profit
      - Decrease of energy or raw materials
  - Indirect social benefits
    - Level of social benefits
      - Area of influence
      - Field of influence
    - Impact on restructuring of the economy
    - Importance for state defense
  - Conformity with the development strategy of RS





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# Medicine: Breast Cancer Risk Assessment



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FORS

multi-attribute decision models in health care, International Journal of Medical Informatics 58-59, 191-205, 2000.







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Bohanec, M., Messéan, A., Scatasta, S., Angevin, F., Griffiths, B., Krogh, P.H., Žnidaršič, M., Džeroski, S.: A qualitative multi-attribute model for economic and ecological assessment of genetically modified crops. *Ecological Modelling* 215, 247-261, 2008.



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Contents lists available at SciVerse ScienceDirect

**Ecological Indicators** 



journal homepage: www.elsevier.com/locate/ecolind

### Assessing innovative cropping systems with DEXiPM, a qualitative multi-criteria assessment tool derived from DEXi

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#### ARTICLE INFO

Article history: Received 6 May 2011 Received in revised form 14 November 2011 Accepted 14 November 2011

Keywords: Cropping system Integrated pest management Sustainability assessment Ex ante Qualitative Multi-Attribute Decision Models DEXi

#### ABSTRACT

Modern intensive agriculture has to face the challenge of feeding the world's growing population while reducing its environmental impacts. Assessing in an *ex ante* way the sustainability of innovative cropping systems will increase the efficiency of the innovation process. To this aim, DEXiPM (DEXi Pest Management) has been developed for *ex ante* assessment of the sustainability of arable cropping systems, particularly integrated crop management systems with a limited use of pesticides. It has 75 basic indicators describing the cropping system and the context of the assessment, and 86 aggregated indicators, assessing the usual three dimensions of sustainability in terms of social, environmental and economic issues. DEXiPM was implemented to assess and compare current and innovative winter crop- and maize-based cropping systems for a French region. The evaluation results showed that innovative cropping systems with a limited use of pesticides can have a better overall sustainability, despite the fact that some of the indicators can be negatively impacted. DEXiPM is a relevant tool to evaluate the sustainability of actual cropping systems, to diagnose their strong and weak points and, on this basis, to encourage discussions during the design of innovative cropping systems that will afterwards be tested in fields. The design of DEXiPM is also based on a state of the art on agricultural sustainability which led to point out



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# **Traffic Control Center**





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driver

O R S

# Assessment of Reputation Risk in Banks

# **FP7 ICT** 2010-2013

OR

#### Large scale information extraction and integration infrastructure for supporting financial decision making

Bohanec, M., Aprile, G., Costante, M., Foti, M., Trdin, N.: A hierarchical multi-attribute model for bank reputational risk assessment. *DSS 2.0 - Supporting Decision Making with New Technologies* (eds. Phillips-Wren, G., et al.), Amsterdam: IOS Press, 92-103, 2014.



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# **DEX: Experience**

- Suitable problems:
  - sorting/classification problems
  - difficult problems (many attributes and/or many alternatives)
  - problems that require human judgment, analysis, justification and explanation
  - problems with prevailing qualitative (rather than quantitative) indicators
  - finding solutions requires expert knowledge (decision rules)
  - uncertainty (incomplete knowledge, imprecise or missing data)
- Characteristics:
  - relatively simple and fast development of models
  - qualitative models are less precise/discriminative than quantitative
  - thus less suitable for choosing and ranking
- Trend: from decision to evaluation systems



# Summary

- DEX:
  - Multi-Attribute decision modeling methodology
  - A pioneering approach, combining multi-criteria decision modeling with rule-based expert systems
- Contributions:
  - Scientific, technical and practical
  - Three generations of software: DECMAK, DEX, DEXi
  - Hundreds of real-life applications
- Status:
  - 30+ years old, but alive: internationally recognized, actively used in new projects, taught in schools, still developing
- Future:
  - DEXi software: maintenance
  - Development of new, extended, more powerful methodology
  - Implementation on new architectures (software library; java, Web, mobile)



Thank you for your attention





